

# Embedded System Design and Synthesis

Robert Dick

<http://robertdick.org/esds/>  
Office: EECS 2417-E

Department of Electrical Engineering and Computer Science  
University of Michigan



Reliable embedded system design and synthesis

Realtime systems  
Scheduling  
Overview of real-time and embedded operating systems  
Embedded application/OS time, power, and energy estimation  
Homework

Algorithm correctness  
Appropriate responses to transient faults  
Appropriate responses to permanent faults

## Types of reliability

- Algorithm correctness: Does the specification have the desired properties?
- Robustness in the presence of transient faults: Can the system continue to operate correctly despite temporary errors?
- Robustness in the presence of permanent faults: Can the system continue to operate correctly in the presence of permanent errors?

3

Robert Dick

Embedded System Design and Synthesis

Reliable embedded system design and synthesis

Realtime systems  
Scheduling

Overview of real-time and embedded operating systems  
Embedded application/OS time, power, and energy estimation  
Homework

Algorithm correctness

Appropriate responses to transient faults  
Appropriate responses to permanent faults

## Conventional software testing

- Implement and test
- Number of tests bounded but number of inputs huge
- Imperfect coverage

5

Robert Dick

Embedded System Design and Synthesis

Reliable embedded system design and synthesis

Realtime systems  
Scheduling

Overview of real-time and embedded operating systems  
Embedded application/OS time, power, and energy estimation  
Homework

Algorithm correctness

Appropriate responses to transient faults  
Appropriate responses to permanent faults

## Model checking

- Use finite state system representation
- Use exhaustive state space exploration to guarantee desired properties hold for all possible paths
- Guarantees properties
- Difficulty with variables that can take on many values
  - Symbolic techniques can improve this
- Difficulty with large number of processes

6

Robert Dick

Embedded System Design and Synthesis

Reliable embedded system design and synthesis

Realtime systems  
Scheduling

Overview of real-time and embedded operating systems  
Embedded application/OS time, power, and energy estimation  
Homework

Algorithm correctness

Appropriate responses to transient faults  
Appropriate responses to permanent faults

## Critical barriers to use

- For simple systems, manual proofs possible
- For very complex systems, state space exploration intractable
- May require new, more formal, specification language

7

Robert Dick

Embedded System Design and Synthesis

Reliable embedded system design and synthesis

Realtime systems  
Scheduling

Overview of real-time and embedded operating systems  
Embedded application/OS time, power, and energy estimation  
Homework

Algorithm correctness

Appropriate responses to transient faults  
Appropriate responses to permanent faults

## Overcoming barriers to use

- Automatic abstraction techniques permitting use on more complex systems
  - Difficult problem
- Target moderate-complexity systems where reliability is important
  - Medical devices
  - Transportation devices
  - Electronic commerce applications
- Give users a high-level language that is actually easier to use than their current language, and provide a path to a language used in existing model checkers

8

Robert Dick

Embedded System Design and Synthesis

## Cross-talk

- Shielding
- Bus encoding

10

Robert Dick

Embedded System Design and Synthesis

## Particle impact

- Temporal redundancy
- Structural redundancy
- Voltage control

11

Robert Dick

Embedded System Design and Synthesis

## Random background offset charge

- Improvements to fabrication
- Temporal redundancy
- Structural redundancy

12

Robert Dick

Embedded System Design and Synthesis

## Temperature-induced timing faults

- Preemptive throttling
- Global planning

13

Robert Dick

Embedded System Design and Synthesis

## Checkpointing: a tool for robustness in the presence of transient faults

- Periodically store system state
- On fault detection, roll back to known-good state
- Should system-wide or incremental, as-needed restores be used?
- When should checkpoints be taken?

14

Robert Dick

Embedded System Design and Synthesis

## Electromigration

- Reduce temperature
- Reduce current
- Spatial redundancy

16

Robert Dick

Embedded System Design and Synthesis

## Manufacturing defects

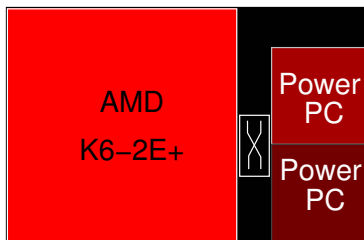
- Spatial redundancy

## Example lifetime failure aware synthesis flow

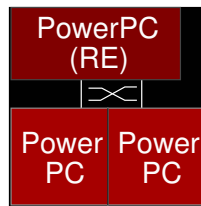
Changyun Zhu, Z. P. Gu, Robert P. Dick, and Li Shang. Reliable multiprocessor system-on-chip synthesis. In *Proc. Int. Conf. Hardware/Software Codesign and System Synthesis*, pages 239–244, October 2007

- Use temperature reduction and spatial redundancy to increase system MTTF
- System MTTF: the expected amount of time an MPSoC will operate, possibly in the presence of component faults, before its performance drops below some designer-specified constraint or it is no longer able to meet its functionality requirements

## Motivating example for reliability optimization

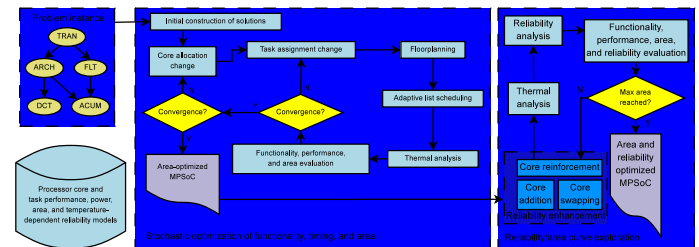


Solution I



Solution II

## Reliability optimization flow



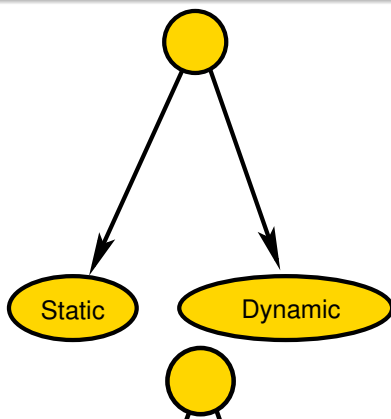
## Lifetime reliability optimization challenges

- Accurate reliability models
- Efficient system-level reliability models
- Efficient fault detection and recovery solutions
- Optimization

## Importance of understanding fault class

- Many reliability techniques attempt to deal with arbitrary fault processes
- However, the properties of the fault process most significant for a particular application may be important
  - Considering them can allow more efficient and reliable designs

## Taxonomy of real-time systems



## Static

- Task arrival times can be predicted.
- Static (compile-time) analysis possible.
- Allows good resource usage (low processor idle time proportions).
- Sometimes designers shoehorn dynamic problems into static formulations allowing a good solution to the wrong problem.

## Dynamic

- Task arrival times unpredictable.
- Static (compile-time) analysis possible only for simple cases.
- Even then, the portion of required processor utilization efficiency goes to 0.693.
- In many real systems, this is very difficult to apply in reality (more on this later).
- Use the right tools but don't over-simplify, e.g.,  
    We assume, without loss of generality, that all tasks are independent.

If you do this people will make jokes about you.

## Soft real-time

- More slack in implementation
- Timing may be suboptimal without being incorrect
- Problem formulation can be much more complicated than hard real-time
- Two common (and one uncommon) methods of dealing with non-trivial soft real-time system requirements
  - Set somewhat loose hard timing constraints
  - Informal design and testing
  - Formulate as optimization problem

## Hard real-time

- Difficult problem. Some timing constraints inflexible.
- Simplifies problem formulation.

## Periodic

- Each task (or group of tasks) executes repeatedly with a particular period.
- Allows some nice static analysis techniques to be used.
- Matches characteristics of many real problems...
- ... and has little or no relationship with many others that designers try to pretend are periodic.

## Periodic → Single-rate

- One period in the system.
- Simple.
- Inflexible.
- This is how a *lot* of wireless sensor networks are implemented.

36

Robert Dick

Embedded System Design and Synthesis

## Periodic → Multirate

- Multiple periods.
- Can use notion of circular time to simplify static (compile-time) schedule analysis E. L. Lawler and D. E. Wood. Branch-and-bound methods: A survey. *Operations Research*, pages 699–719, July 1966.
- Co-prime periods leads to analysis problems.

37

Robert Dick

Embedded System Design and Synthesis

## Periodic → Other

- It is possible to have tasks with deadlines less than, equal to, or greater than their periods.
- Results in multi-phase, circular-time schedules with multiple concurrent task instances.
  - If you ever need to deal with one of these, see me (take my code). This class of scheduler is nasty to code.

38

Robert Dick

Embedded System Design and Synthesis

## Aperiodic

- Also called sporadic, asynchronous, or reactive
- Implies dynamic
- Bounded arrival time interval permits resource reservation
- Unbounded arrival time interval impossible to deal with for any resource-constrained system

39

Robert Dick

Embedded System Design and Synthesis

## Definitions

- Task
- Processor
- Graph representations
- Deadline violation
- Cost functions

41

Robert Dick

Embedded System Design and Synthesis

## Task

- Some operation that needs to be carried out
- Atomic completion: A task is all done or it isn't
- Non-atomic execution: A task may be interrupted and resumed

42

Robert Dick

Embedded System Design and Synthesis

## Processor

- Processors execute tasks
- Distributed systems
  - Contain multiple processors
  - Inter-processor communication has impact on system performance
  - Communication is challenging to analyze
- One processor type: Homogeneous system
- Multiple processor types: Heterogeneous system

43

Robert Dick

Embedded System Design and Synthesis

## Task/processor relationship

WC exec time (s)

Tooth	7.7E-6	...	
Road	330E-9	...	
FIR	4.1E-6	...	
Matrix	310E-3	...	

IBMPowerPC 405GP 266 MHz  
 IDT79RC32364 100 MHz  
 Imsys Cjip 40 MHz

Relationship between tasks, processors, and costs  
 E.g., power consumption or worst-case execution time

44

Robert Dick

Embedded System Design and Synthesis

## Cost functions

- Mapping of real-time system design problem solution instance to cost value
- I.e., allows price, or hard deadline violation, of a particular multi-processor implementation to be determined

45

Robert Dick

Embedded System Design and Synthesis

## Back to real-time problem taxonomy: Jagged edges

- Some things dramatically complicate real-time scheduling
- These are horrific, especially when combined
  - Data dependencies
  - Unpredictability
  - Distributed systems
- These are irksome
  - Heterogeneous processors
  - Preemption

46

Robert Dick

Embedded System Design and Synthesis

## Central areas of real-time study

- Allocation, assignment and **scheduling**
- Operating systems and **scheduling**
- Distributed systems and **scheduling**
- Scheduling is at the core of real-time systems study**

48

Robert Dick

Embedded System Design and Synthesis

## Allocation, assignment, and scheduling

How does one best

- Analyze problem instance specifications
  - E.g., worst-case task execution time
- Select (and build) hardware components
- Select and produce software
- Decide which processor will be used for each task
- Determine the time(s) at which all tasks will execute

49

Robert Dick

Embedded System Design and Synthesis

## Allocation, assignment, and scheduling

- In order to efficiently and (when possible) optimally minimize
  - Price, power consumption, soft deadline violations
- Under hard timing constraints
- Providing guarantees whenever possible
- For all the different classes of real-time problem classes

This is what I did for a Ph.D.

## Operating systems and scheduling

How does one best design operating systems to

- Support sufficient detail in workload specification to allow good control, e.g., over scheduling, without increasing design error rate
- Design operating system schedulers to support real-time constraints?
- Support predictable costs for task and OS service execution

## Distributed systems and scheduling

How does one best dynamically control

- The assignment of tasks to processing nodes...
- ... and their schedules

for systems in which computation nodes may be separated by vast distances such that

- Task deadline violations are bounded (when possible)...
- ... and minimized when no bounds are possible

## The value of formality: Optimization and costs

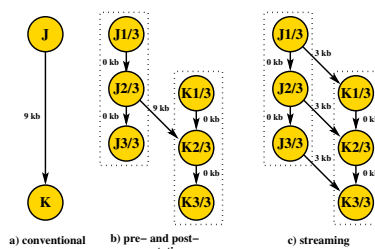
- The design of a real-time system is fundamentally a cost optimization problem
- Minimize costs under constraints while meeting functionality requirements
  - Slight abuse of notation here, functionality requirements are actually just constraints
- Why view problem in this manner?
- Without having a concrete definition of the problem
  - How is one to know if an answer is correct?
  - More subtly, how is one to know if an answer is optimal?

## Optimization

Thinking of a design problem in terms of optimization gives design team members objective criterion by which to evaluate the impact of a design change on quality.

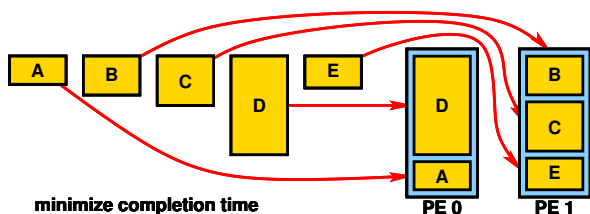
Know whether your design changes are taking you in a good direction

## Graph extensions



Allows pipelining and pre/post-computation  
 In contrast with book, not difficult to use if conversion automated

## Problem definition



minimize completion time

- Given a set of tasks,
- a cost function,
- and a set of resources,
- decide the exact time each task will execute on each resource

## Types of scheduling problems

- Discrete time – Continuous time
- Hard deadline – Soft deadline
- Unconstrained resources – Constrained resources
- Uni-processor – Multi-processor
- Homogeneous processors – Heterogeneous processors
- Free communication – Expensive communication
- Independent tasks – Precedence constraints
- Homogeneous tasks – Heterogeneous tasks
- One-shot – Periodic
- Single rate – Multirate
- Non-preemptive – Preemptive
- Off-line – On-line

## Discrete vs. continuous timing

System-level: Continuous

- Operations are not small integer multiples of the clock cycle

High-level: Discrete

- Operations are small integer multiples of the clock cycle

Implications:

- System-level scheduling is more complicated...
- ... however, high-level also very difficult.
- Can we solve this by quantizing time? Why or why not?

## Hard deadline – Soft deadline

Tasks may have hard or soft deadlines

- Hard deadline
  - Task must finish by given time or schedule invalid
- Soft deadline
  - If task finishes after given time, schedule cost increased

## Real-time – Best effort

- Why make decisions about system implementation statically?
  - Allows easy timing analysis, hard real-time guarantees
- If a system doesn't have hard real-time deadlines, resources can be more efficiently used by making late, dynamic decisions
- Can combine real-time and best-effort portions within the same specification
  - Reserve time slots
  - Take advantage of slack when tasks complete sooner than their worst-case finish times

## Unconstrained – Constrained resources

- Unconstrained resources
  - Additional resources may be used at will
- Constrained resources
  - Limited number of devices may be used to execute tasks



## Uni-processor – Multi-processor

- Uni-processor
  - All tasks execute on the same resource
  - This can still be somewhat challenging
  - However, sometimes in  $\mathcal{P}$
- Multi-processor
  - There are multiple resources to which tasks may be scheduled
- Usually  $\mathcal{NP}$ -complete

64

Robert Dick

Embedded System Design and Synthesis

## Homogeneous – Heterogeneous processors

- Homogeneous processors
  - All processors are the same type
- Heterogeneous processors
  - There are different types of processors
  - Usually  $\mathcal{NP}$ -complete

65

Robert Dick

Embedded System Design and Synthesis

## Free – Expensive communication

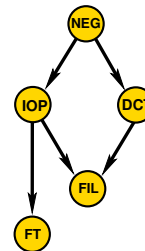
- Free communication
  - Data transmission between resources has no time cost
- Expensive communication
  - Data transmission takes time
  - Increases problem complexity
  - Generation of schedules for communication resources necessary
  - Usually  $\mathcal{NP}$ -complete

66

Robert Dick

Embedded System Design and Synthesis

## Independent tasks – Precedence constraints



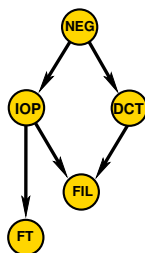
- Independent tasks: No previous execution sequence imposed
- Precedence constraints: Weak order on task execution order

67

Robert Dick

Embedded System Design and Synthesis

## Homogeneous – Heterogeneous tasks



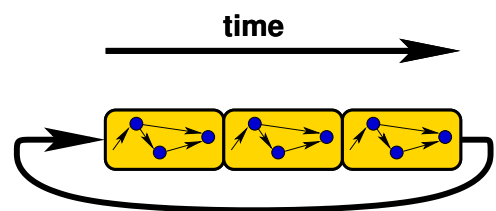
- Homogeneous tasks: All tasks are identical
- Heterogeneous tasks: Tasks differ

68

Robert Dick

Embedded System Design and Synthesis

## One-shot – Periodic



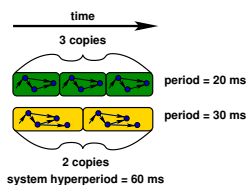
- One-shot: Assume that the task set executes once
- Periodic: Ensure that the task set can repeatedly execute at some period

69

Robert Dick

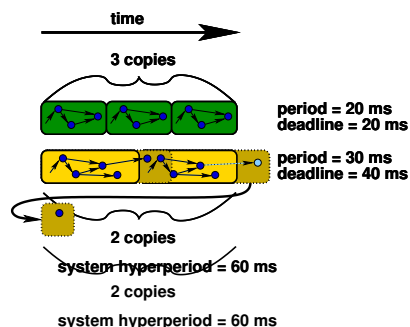
Embedded System Design and Synthesis

## Single rate – Multirate



- Single rate: All tasks have the same period
- Multirate: Different tasks have different periods
  - Complicates scheduling
  - Can copy out to the least common multiple of the periods (hyperperiod)

## Periodic graphs



## Aperiodic/sporadic graphs

- No precise periods imposed on task execution
- Useful for representing reactive systems
- Difficult to guarantee hard deadlines in such systems
  - Possible if minimum inter-arrival time known

## Periodic vs. aperiodic

### Periodic applications

- Power electronics
  - Engine controllers
  - Brake controllers
- Many multimedia applications
  - Video frame rate
  - Audio sample rate
- Many digital signal processing (DSP) applications

However, devices which react to unpredictable external stimuli have aperiodic behavior

Many applications contain periodic and aperiodic components

## Aperiodic to periodic

Can design periodic specifications that meet requirements posed by aperiodic/sporadic specifications

- Some resources will be wasted

Example:

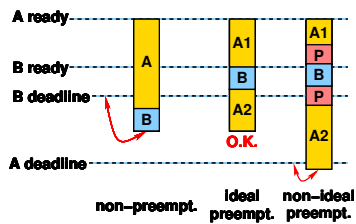
- At most one aperiodic task can arrive every 50 ms
- It must complete execution within 100 ms of its arrival time

## Aperiodic to periodic

- Can easily build a periodic representation with a deadline and period of 50 ms
  - Problem, requires a 50 ms execution time when 100 ms should be sufficient
- Can use overlapping graphs to allow an increase in execution time
  - Parallelism required

The main problem with representing aperiodic problems with periodic representations is that the tradeoff between deadline and period must be made at design/synthesis time

## Non-preemptive – Preemptive



- Non-preemptive: Tasks must run to completion
- Ideal preemptive: Tasks can be interrupted without cost
- Non-ideal preemptive: Tasks can be interrupted with cost

## Off-line – On-line

### Off-line

- Schedule generated before system execution
- Stored, e.g., in dispatch table. for later use
- Allows strong design/synthesis/compile-time guarantees to be made
- Not well-suited to strongly reactive systems

### On-line

- Scheduling decisions made during the execution of the system
- More difficult to analyze than off-line
  - Making hard deadline guarantees requires high idle time
  - No known guarantee for some problem types
- Well-suited to reactive systems

## Hardware-software co-synthesis scheduling

Automatic allocation, assignment, and scheduling of system-level specification to hardware and software

Scheduling problem is hard

- Hard and soft deadlines
- Constrained resources, but resources unknown (cost functions)
- Multi-processor
- Strongly heterogeneous processors and tasks
  - No linear relationship between the execution times of a tasks on processors

## Hardware-software co-synthesis scheduling

- Expensive communication
  - Complicated set of communication resources
- Precedence constraints
- Periodic
- Multirate
- Strong interaction between  $\mathcal{NP}$ -complete allocation-assignment and  $\mathcal{NP}$ -complete scheduling problems
- Will revisit problem later in course if time permits

## Behavioral synthesis scheduling

- Difficult real-world scheduling problem
  - Not multirate
  - Discrete notion of time
  - Generally less heterogeneity among resources and tasks
- What scheduling algorithms should be used for these problems?

## Scheduling methods

- Clock
- Weighted round-robin
- List scheduling
- Priority
  - EDF, LST
  - Slack
  - Multiple costs

## Scheduling methods

- MILP
- Force-directed
- Frame-based
- PSGA
- RMS

83

Robert Dick

Embedded System Design and Synthesis

## Clock-driven scheduling

Clock-driven: Pre-schedule, repeat schedule  
Music box:

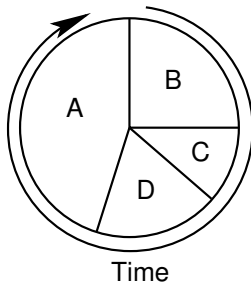
- Periodic
- Multi-rate
- Heterogeneous
- Off-line
- Clock-driven

84

Robert Dick

Embedded System Design and Synthesis

## Weighted round robin



Weighted round-robin: Time-sliced with variable time slots

85

Robert Dick

Embedded System Design and Synthesis

## List scheduling

- Pseudo-code:
  - Keep a list of ready jobs
  - Order by priority metric
  - Schedule
  - Repeat
- Simple to implement
- Can be made very fast
- Difficult to beat quality

86

Robert Dick

Embedded System Design and Synthesis

## Priority-driven

- Impose linear order based on priority metric
- Possible metrics
  - Earliest start time (EST)
  - Latest start time
    - Danger! LST also stands for least slack time.
  - Shortest execution time first (SETF)
  - Longest execution time first (LETF)
  - Slack (LFT - EFT)

87

Robert Dick

Embedded System Design and Synthesis

## List scheduling

- Assigns priorities to nodes
- Sequentially schedules them in order of priority
- Usually very fast
- Can be high-quality
- Prioritization metric is important

88

Robert Dick

Embedded System Design and Synthesis

## Prioritization

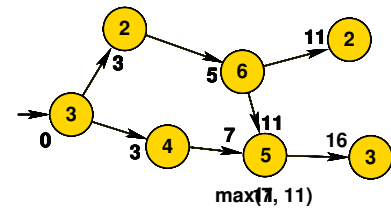
- As soon as possible (ASAP)
- As late as possible (ALAP)
- Slack-based
- Dynamic slack-based
- Multiple considerations

89

Robert Dick

Embedded System Design and Synthesis

## As soon as possible (ASAP)



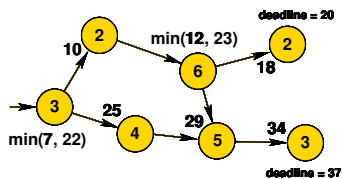
- From root, topological sort on the precedence graph
- Propagate execution times, taking the max at reconverging paths
- Schedule in order of increasing earliest start time (EST)

90

Robert Dick

Embedded System Design and Synthesis

## As late as possible (ALAP)



- From deadlines, topological sort on the precedence graph
- Propagate execution times, taking the min at reconverging paths
- Consider precedence-constraint satisfied tasks
  - Schedule in order of increasing latest start time (LST)

91

Robert Dick

Embedded System Design and Synthesis

## Slack-based

- Compute EFT, LFT
- For all tasks, find the difference,  $LFT - EFT$
- This is the *slack*
- Schedule precedence-constraint satisfied tasks in order of increasing slack
- Can recompute slack each step, expensive but higher-quality result
  - Dynamic critical path scheduling

92

Robert Dick

Embedded System Design and Synthesis

## Multiple considerations

- Nothing prevents multiple prioritization methods from being used
- Try one method, if it fails to produce an acceptable schedule, reschedule with another method

93

Robert Dick

Embedded System Design and Synthesis

## Effective release times

- Ignore the book on this
  - Considers simplified, uniprocessor, case
- Use EFT, LFT computation
- Example?

94

Robert Dick

Embedded System Design and Synthesis

## EDF, LST optimality

- EDF optimal if zero-cost preemption, uniprocessor assumed
  - Why?
  - What happens when preemption has cost?
- Same is true for slack-based list scheduling in absence of preemption cost

95

Robert Dick

Embedded System Design and Synthesis

## Breaking EDF, LST optimality

- Non-zero preemption cost
- Multiprocessor
- Why?

96

Robert Dick

Embedded System Design and Synthesis

## Multi-rate tricks

- Contract deadline
  - Usually safe
- Contract period
  - Sometimes safe
- Consequences?

97

Robert Dick

Embedded System Design and Synthesis

## Linear programming

- Minimize a linear equation subject to linear constraints
  - In  $\mathcal{P}$
- Mixed integer linear programming: One or more variables discrete
  - $\mathcal{NP}$ -complete
- Many good solvers exist
- Don't rebuild the wheel

98

Robert Dick

Embedded System Design and Synthesis

## MILP scheduling

$P$  the set of tasks

$t_{max}$  maximum time

$start(p, t)$  1 if task  $p$  starts at time  $t$ , 0 otherwise

$D$  the set of execution delays

$E$  the set of precedence constraints

$$t_{start}(p) = \sum_{t=0}^{t_{max}} t \cdot start(p, t) \text{ the start time of } p$$

99

Robert Dick

Embedded System Design and Synthesis

## MILP scheduling

Each task has a unique start time

$$\forall p \in P, \sum_{t=0}^{t_{max}} start(p, t) = 1$$

Each task must satisfy its precedence constraints and timing delays

$$\forall \{p_i, p_j\} \in E, \sum_{t=0}^{t_{max}} t_{start}(p_i) \geq t_{start}(p_j) + d_j$$

Other constraints may exist

- Resource constraints
- Communication delay constraints

100

Robert Dick

Embedded System Design and Synthesis

## MILP scheduling

- Too slow for large instances of  $\mathcal{NP}$ -complete scheduling problems
- Numerous optimization algorithms may be used for scheduling
- List scheduling is one popular solution
- Integrated solution to allocation/assignment/scheduling problem possible
- Performance problems exist for this technique

101

Robert Dick

Embedded System Design and Synthesis

## Force directed scheduling

- P. G. Paulin and J. P. Knight. Force-directed scheduling for the behavioral synthesis of ASICs. *IEEE Trans. Computer-Aided Design of Integrated Circuits and Systems*, 8(6):661–679, June 1989
- Calculate EST and LST of each node
- Determine the force on each vertex at each time-step
- Force: Increase in probabilistic concurrency
  - Self force
  - Predecessor force
  - Successor force

102

Robert Dick

Embedded System Design and Synthesis

## Self force

$F_i$  all slots in time frame for  $i$

$F'_i$  all slots in new time frame for  $i$

$D_t$  probability density (sum) for slot  $t$

$\delta D_t$  change in density (sum) for slot  $t$  resulting from scheduling

self force

$$A = \sum_{t \in F_a} D_t \cdot \delta D_t$$

103

Robert Dick

Embedded System Design and Synthesis

## Predecessor and successor forces

**pred** all predecessors of node under consideration

**succ** all successors of node under consideration

predecessor force

$$B = \sum_{b \in \text{pred}} \sum_{t \in F_b} D_t \cdot \delta D_t$$

successor force

$$C = \sum_{c \in \text{succ}} \sum_{t \in F_c} D_t \cdot \delta D_t$$

104

Robert Dick

Embedded System Design and Synthesis

## Intuition

total force:  $A + B + C$

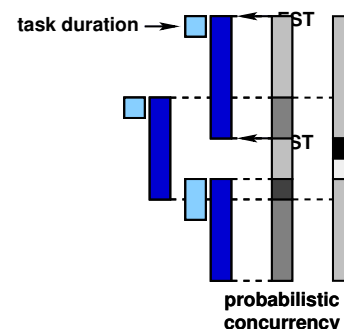
- Schedule operation and time slot with minimal total force
  - Then recompute forces and schedule the next operation
- Attempt to balance concurrency during scheduling

105

Robert Dick

Embedded System Design and Synthesis

## Force directed scheduling



106

Robert Dick

Embedded System Design and Synthesis

## Force directed scheduling

- Limitations?
- What classes of problems may this be used on?

107

Robert Dick

Embedded System Design and Synthesis

## Implementation: Frame-based scheduling

- Break schedule into (usually fixed) frames
  - Large enough to hold a long job
    - Avoid preemption
- Evenly divide hyperperiod
- Scheduler makes changes at frame start
- Network flow formulation for frame-based scheduling
- Could this be used for on-line scheduling?

108

Robert Dick

Embedded System Design and Synthesis

## Problem space genetic algorithm

- Let's finish off-line scheduling algorithm examples on a bizarre example
- Use conventional scheduling algorithm
- Transform problem instance
- Solve
- Validate
- Evolve transformations

109

Robert Dick

Embedded System Design and Synthesis

## Rate monotonic scheduling (RMS)

- Single processor
- Independent tasks
- Differing arrival periods
- Schedule in order of increasing periods
- No fixed-priority schedule will do better than RMS
- Guaranteed valid for loading  $\leq \ln 2 = 0.69$
- For loading  $> \ln 2$  and  $< 1$ , correctness unknown
- Usually works up to a loading of 0.88

110

Robert Dick

Embedded System Design and Synthesis

## Rate monotonic scheduling

### Main idea

- 1973, Liu and Layland derived optimal scheduling algorithm(s) for this problem
- Schedule the job with the smallest period (period = deadline) first
- Analyzed worst-case behavior on any task set of size  $n$
- Found utilization bound:  $U(n) = n \cdot (2^{1/n} - 1)$
- 0.828 at  $n = 2$
- As  $n \rightarrow \infty$ ,  $U(n) \rightarrow \log 2 = 0.693$
- Result: For any problem instance, if a valid schedule is possible, the processor need never spend more than 31% of its time idle

111

Robert Dick

Embedded System Design and Synthesis

## Optimality and utilization for limited case

- Simply periodic: All task periods are integer multiples of all lesser task periods
- In this case, RMS/DMS optimal with utilization 1
- However, this case rare in practice
- Remains feasible, with decreased utilization bound, for in-phase tasks with arbitrary periods

112

Robert Dick

Embedded System Design and Synthesis



## Rate monotonic scheduling

- Constrained problem definition
- Over-allocation often results
- However, in practice utilization of 85%–90% common
  - Lose guarantee
- If phases known, can prove by generating instance

113

Robert Dick

Embedded System Design and Synthesis

## Critical instants

Main idea:

A job's critical instant a time at which all possible concurrent higher-priority jobs are also simultaneously released

Useful because it implies latest finish time

114

Robert Dick

Embedded System Design and Synthesis

## Definitions

- Period:  $T$ .
- Execution time:  $C$ .
- Process:  $i$ .
- Utilization:  $U = \sum_{i=1}^m \frac{C_i}{T_i}$ .
- Assume Task 1 is higher priority than Task 2, and thus  $T_1 < T_2$ .

115

Robert Dick

Embedded System Design and Synthesis

## Case 1 I

All instances of higher-priority tasks released before end of lower-priority task period complete before end of lower-priority task period.

- 1  $C_1 \leq T_2 - T_1 \left\lceil \frac{T_2}{T_1} \right\rceil$ .
- 2 I.e., the execution time of Task 1 is less than or equal to the period of Task 2 minus the total time spent within the periods of instances of Task 1 finishing within Task 2's period.
- 3 Now, let's determine the maximum execution time of Task 2 as a function of all other variables.
- 4  $C_{2,max} = T_2 - C_1 \left\lceil \frac{T_2}{T_1} \right\rceil$ .

116

Robert Dick

Embedded System Design and Synthesis

## Case 1 II

- 5 I.e., the maximum execution time of Task 2 is the period of Task 2 minus the total execution time of instances of Task 1 released within Task 2's period.

117

Robert Dick

Embedded System Design and Synthesis

## Case 1 III

- 6 In this case,

$$\begin{aligned}
 U &= U_1 + U_2 \\
 &= \frac{C_1}{T_1} + \frac{C_{2,max}}{T_2} \\
 &= \frac{C_1}{T_1} + \frac{T_2 - C_1 \left\lceil \frac{T_2}{T_1} \right\rceil}{T_2} \\
 &= \frac{C_1}{T_1} + 1 - \frac{C_1 \left\lceil \frac{T_2}{T_1} \right\rceil}{T_2} \\
 &= 1 + C_1 \left( \frac{1}{T_1} - \frac{1}{T_2} \left\lceil \frac{T_2}{T_1} \right\rceil \right)
 \end{aligned}$$

- 7 Is  $\frac{1}{T_1} - \frac{1}{T_2} \left\lceil \frac{T_2}{T_1} \right\rceil < 0$ ?

118

Robert Dick

Embedded System Design and Synthesis

## Case 1 IV

- 8 Thus,  $U$  is monotonically decreasing in  $C_1$ .

## Case 2 I

Instances of higher-priority tasks released before end of lower-priority task period complete after end of lower-priority task period.

- 1  $C_1 \geq T_2 - T_1 \left\lfloor \frac{T_2}{T_1} \right\rfloor$ .
- 2  $C_{2,max} = -C_1 \left\lfloor \frac{T_2}{T_1} \right\rfloor + T_1 \left\lfloor \frac{T_2}{T_1} \right\rfloor$ .
- 3  $U = \frac{T_1}{T_2} \left\lfloor \frac{T_2}{T_1} \right\rfloor + C_1 \left( \frac{1}{T_1} - \frac{1}{T_2} \left\lfloor \frac{T_2}{T_1} \right\rfloor \right)$ .

## Minimal $U$

- 1  $C_1 = T_2 - T_1 \left\lfloor \frac{T_2}{T_1} \right\rfloor$ .
- 2  $U = 1 - \frac{T_1}{T_2} \left( \left\lfloor \frac{T_2}{T_1} \right\rfloor - \frac{T_2}{T_1} \right) \left( \frac{T_2}{T_1} - \left\lfloor \frac{T_2}{T_1} \right\rfloor \right)$ .
- 3 Let  $I = \left\lfloor \frac{T_2}{T_1} \right\rfloor$  and
- 4  $f = \frac{T_2}{T_1}$ .
- 5 Then,  $U = 1 - \frac{f(1-f)}{I+f}$ .
- 6 To maximize  $U$ , minimize  $I$ , which can be no smaller than 1.
- 7  $U = 1 - \frac{f(1-f)}{1+f}$ .
- 8 Differentiate to find minima, at  $f = \sqrt{2} - 1$ .
- 9 Thus,  $U_{min} = 2(\sqrt{2} - 1) \approx 0.83$ .
- 10 Is this the minimal  $U$ ? Are we done?

## Notes on RMS

- DMS better than or equal RMS when deadline  $\neq$  period
- Why not use slack-based?
- What happens if resources are under-allocated and a deadline is missed?

## Scheduling summary

- Scheduling is a huge area
- This lecture only introduced the problem and potential solutions
- Some scheduling problems are easy
- Most useful scheduling problems are hard
  - Committing to decisions makes problems hard: Lookahead required
  - Interdependence between tasks and processors makes problems hard

## Mixing on-line and off-line

- Book mixes off-line and on-line with little warning
- Be careful, actually different problem domains
- However, can be used together
- Superloop (cyclic executive) with non-critical tasks
- Slack stealing
- Processor-based partitioning

## Vehicle routing

- Low-price, slow, ARM-based system
- Long-term shortest path computation
- Greedy path calculation algorithm available, non-preemptable
- Don't make the user wait
  - Short-term next turn calculation
- 200 ms timer available

126

Robert Dick

Embedded System Design and Synthesis

## Mixing on-line and off-line

- Slack stealing
- Processor-based partitioning

127

Robert Dick

Embedded System Design and Synthesis

## Bizarre scheduling idea

- Scheduling and validity checking algorithms considered so far operate in time domain
- This is a somewhat strange idea
- Think about it and tell/email me if you have any thoughts on it
- Could one very quickly generate a high-quality real-time off-line multi-rate periodic schedule by operating in the frequency domain?
- If not, why not?
- What if the deadlines were soft?

128

Robert Dick

Embedded System Design and Synthesis

## Example problem: Static scheduling

- What is an FPGA?
- Why should real-time systems designers care about them?
- Multiprocessor static scheduling
- No preemption
- No overhead for subsequent execution of tasks of same type
- High cost to change task type
- Scheduling algorithm?

129

Robert Dick

Embedded System Design and Synthesis

## Problem: Uniprocessor independent task scheduling

- Problem
  - Independent tasks
  - Each has a period = hard deadline
  - Zero-cost preemption
- How to solve?

130

Robert Dick

Embedded System Design and Synthesis

## Essential features of RTOSs

- Provides real-time scheduling algorithms or primitives
- Bounded execution time for OS services
  - Usually implies preemptive kernel
  - E.g., Linux can spend milliseconds handling interrupts, especially disk access

132

Robert Dick

Embedded System Design and Synthesis

## Threads

- Threads vs. processes: Shared vs. unshared resources
- OS impact: Windows vs. Linux
- Hardware impact: MMU

133

Robert Dick

Embedded System Design and Synthesis

## Threads vs. processes

- Threads: Low context switch overhead
- Threads: Sometimes the only real option, depending on hardware
- Processes: Safer, when hardware provides support
- Processes: Can have better performance when IPC limited

134

Robert Dick

Embedded System Design and Synthesis

## Software implementation of schedulers

- TinyOS
- Light-weight threading executive
- $\mu$ C/OS-II
- Linux
- Static list scheduler

135

Robert Dick

Embedded System Design and Synthesis

## TinyOS

- Most behavior event-driven
- High rate  $\rightarrow$  Livelock
- Research schedulers exist

136

Robert Dick

Embedded System Design and Synthesis

## BD threads

- Brian Dean: Microcontroller hacker
- Simple priority-based thread scheduling executive
- Tiny footprint (fine for AVR)
- Low overhead
- No MMU requirements

137

Robert Dick

Embedded System Design and Synthesis

## $\mu$ C/OS-II

- Similar to BD threads
- More flexible
- Bigger footprint

138

Robert Dick

Embedded System Design and Synthesis

## Old Linux scheduler

- Single run queue
- $O(n)$  scheduling operation
- Allows dynamic goodness function

## $O(1)$ scheduler in Linux 2.6

- Written by Ingo Molnar
- Splits run queue into two queues prioritized by goodness
- Requires static goodness function
  - No reliance on running process
- Compatible with preemptible kernel

## Real-time Linux

- Run Linux as process under real-time executive
- Complicated programming model
- RTAI (Real-Time Application Interface) attempts to simplify
  - Colleagues still have problems at  $> 18$  kHz control period

## Real-time operating systems

- Embedded vs. real-time
- Dynamic memory allocation
- Schedulers: General-purpose vs. real-time
- Timers and clocks: Relationship with HW

## Collaborators on project

Princeton  
 Niraj K. Jha

NEC Labs America  
 Ganesh Lakshminarayana  
 Anand Raghunathan

## Introduction

- Real-Time Operating Systems are often used in embedded systems
- They simplify use of hardware, ease management of multiple tasks, and adhere to real-time constraints
- Power is important in many embedded systems with RTOSs
- RTOSs can consume significant amount of power
- They are re-used in many embedded systems
- They impact power consumed by application software
- RTOS power effects influence system-level design

## Real-time operating systems (RTOS)

- Interaction between HW and SW
  - Rapid response to interrupts
  - HW interface abstraction
- Interaction between different tasks
  - Communication
  - Synchronization
- Multitasking
  - Ideally fully preemptive
  - Priority-based scheduling
  - Fast context switching
  - Support for real-time clock

147

Robert Dick

Embedded System Design and Synthesis

## General-purpose OS stress

- Good average-case behavior
- Providing many services
- Support for a large number of hardware devices

148

Robert Dick

Embedded System Design and Synthesis

## RTOSs stress

- Predictable service execution times
- Predictable scheduling
- Good worst-case behavior
- Low memory usage
- Speed
- Simplicity

149

Robert Dick

Embedded System Design and Synthesis

## Predictability

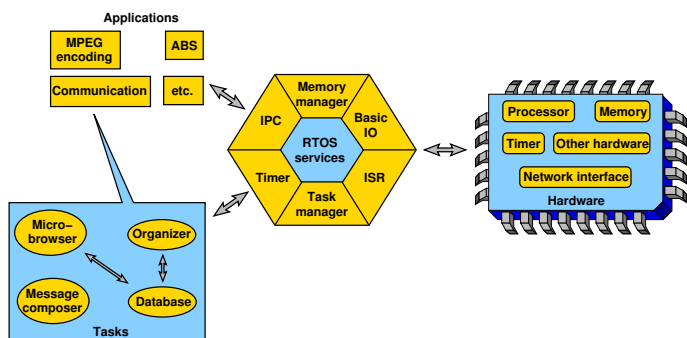
- General-purpose computer architecture focuses on average-case
  - Caches
  - Prefetching
  - Speculative execution
- Real-time embedded systems need predictability
  - Disabling or locking caches is common
  - Careful evaluation of worst-case is essential
  - Specialized or static memory management common

150

Robert Dick

Embedded System Design and Synthesis

## RTOS overview



151

Robert Dick

Embedded System Design and Synthesis

## RTOS power consumption

- Used in several low-power embedded systems
- Need for RTOS power analysis
  - Significant power consumption
  - Impacts application software power
  - Re-used across several applications

152

Robert Dick

Embedded System Design and Synthesis

- K. Ramamritham and J. Stankovic. Scheduling algorithms and operating systems support for real-time systems. *Proc. IEEE*, 82(1):55–67, January 1994
- Giorgio C. Buttazzo. *Hard Real-Time Computing Systems*. Kluwer Academic Publishers, Boston, 2000

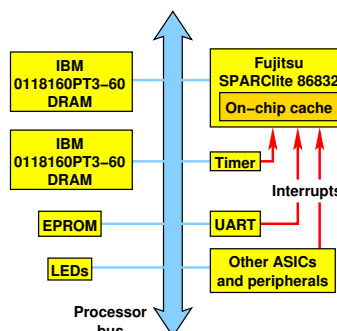
- Vivek Tiwari, Sharad Malik, and Andrew Wolfe. Compilation techniques for low energy: An overview. In *Proc. Int. Symp. Low-Power Electronics*, pages 38–39, October 1994
- Y. Li and J. Henkel. A framework for estimating and minimizing energy dissipation of embedded HW/SW systems. In *Proc. Design Automation Conf.*, pages 188–193, June 1998
- J. J. Labrosse. *MicroC/OS-II*. R & D Books, KS, 1998

Journal version Design Automation Conference 2000 work in the area of RTOS power consumption analysis

- Robert P. Dick, G. Lakshminarayana, A. Raghunathan, and Niraj K. Jha. Analysis of power dissipation in real-time operating systems. *IEEE Trans. Computer-Aided Design of Integrated Circuits and Systems*, 22(5):615–627, May 2003

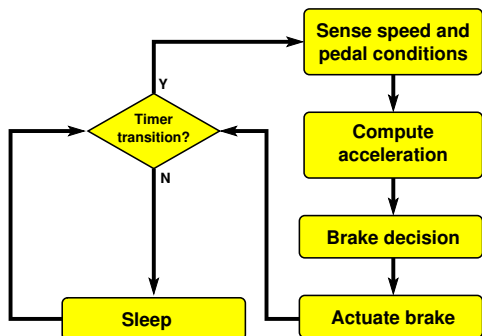
- K. Baynes, C. Collins, E. Fiterman, B. Ganesh, P. Kohout, C. Smit, T. Zhang, and B. Jacob. The performance and energy consumption of three embedded real-time operating systems. In *Proc. Int. Conf. Compilers, Architecture & Synthesis for Embedded Systems*, pages 203–210, November 2001
- T.-K. Tan, A. Raghunathan, and Niraj K. Jha. EMSIM: An energy simulation framework for an embedded operating system. In *Proc. Int. Symp. Circuits & Systems*, pages 464–467, May 2002

- First detailed power analysis of RTOS
  - Proof of concept later used by others
- Applications
  - Low-power RTOS
  - Energy-efficient software architecture
  - Incorporate RTOS effects in system design



- Easy to add new devices
- Cycle-accurate model
- Fujitsu board support library used in model
- $\mu$ C/OS-II RTOS used

## Periodically triggered ABS

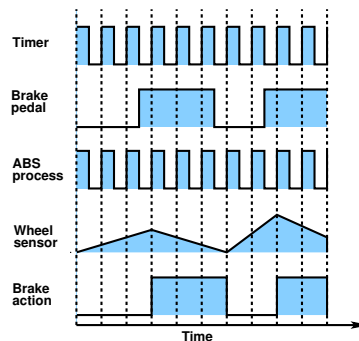


160

Robert Dick

Embedded System Design and Synthesis

## Periodically triggered ABS timing

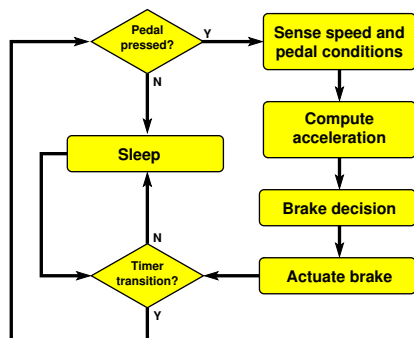


161

Robert Dick

Embedded System Design and Synthesis

## Selectively triggered ABS

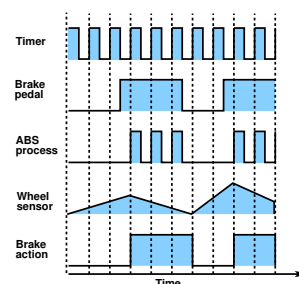


162

Robert Dick

Embedded System Design and Synthesis

## Selectively triggered ABS timing



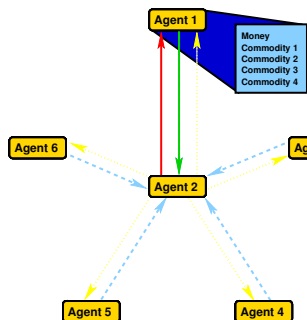
63% reduction in energy and power consumption

163

Robert Dick

Embedded System Design and Synthesis

## Agent example



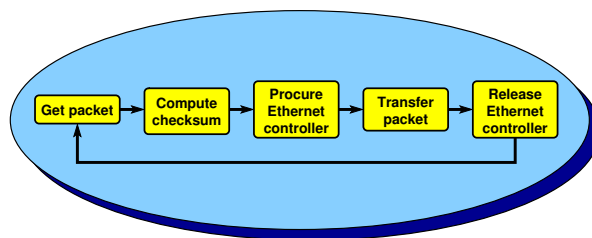
- Advertise
- Bid
- Offer
- Transfer results

164

Robert Dick

Embedded System Design and Synthesis

## Single task network interface



Procuring Ethernet controller has high energy cost

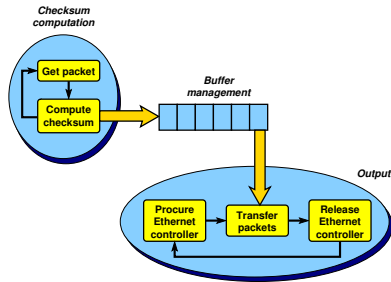
165

Robert Dick

Embedded System Design and Synthesis

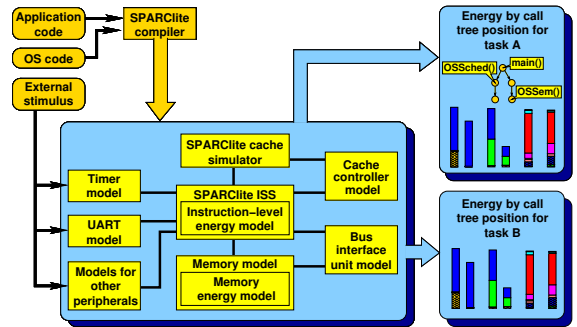


## Multi-tasking network interface



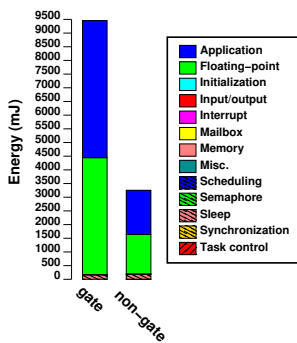
RTOS power analysis suggests process re-organization.  
 21% reduction in energy consumption. Similar power consumption.

## Infrastructure



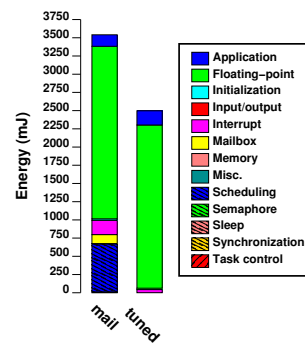
RTOS power analysis suggests process re-organization.  
 21% reduction in energy consumption. Similar power consumption.

## ABS optimization effects



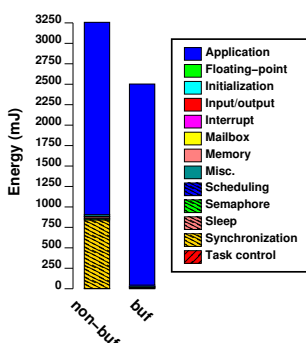
- Redesigned application after using simulator to locate areas where power was wasted
- 63% energy reduction
- 63% power reduction
- RTOS directly accounted for 50% of system energy

## Agent optimization effects



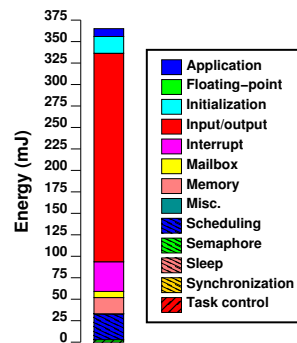
- Mail version used RTOS mailboxes for information transmission
- Tuned version carefully hand-tuned to used shared memory
- Power can be reduced at a cost
  - Increased application software complexity
  - Decreased flexibility

## Ethernet optimization effects



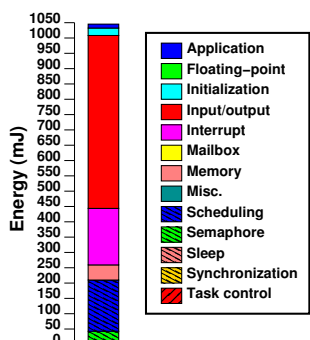
- Determined that synchronization routine cost was high
  - Used RTOS buffering to amortize synchronization costs
- 20.5% energy reduction
- 0.2% power reduction
- RTOS directly accounted for 1% of system energy
  - Energy savings due to improved RTOS use, not reduced RTOS energy

## Mailbox example



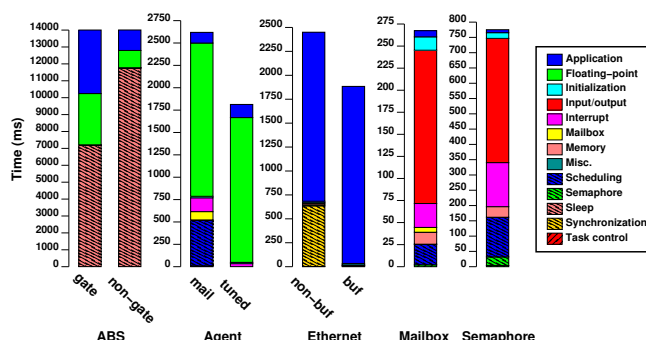
- Rapid mailbox communication between tasks
- RTOS directly accounted for 99% of system energy

## Semaphore example



- Semaphores used for task synchronization
- RTOS directly accounted for 98.7% of system energy

## Time results



## Energy bounds

Service	Minimum energy ( $\mu\text{J}$ )	Maximum energy ( $\mu\text{J}$ )
AgentTask	3.41	4727.88
fptodp	17.46	49.72
BSPInit	3.52	3.52
fstat	16.34	16.34
CPUInit	287.15	287.15
fstat_r	31.26	31.26
GetPsr	0.38	0.55
init_bss	2.86	3.07
GetTbr	0.40	0.53
init_data	4.23	4.37
InitTimer	2.53	2.53
init_timer	18012.10	20347.00
OSCtxSw	46.63	65.65
init_tvcs	1.31	1.31
OSDisableInt	0.84	1.31
...	...	...

## Semaphore example hierarchical call tree

	Function	Energy( $\mu\text{J}$ ) invocation	Energy (%)	Time (ms)	Calls	
realstart	init_tvcs	1.31	0.00	0.00	1	
25.40 mJ total 2.43 %	init_timer	18.01	0.00	0.00	1	
	startup	7.39	0.70	5.57	1	
	do_main	7363.11	0.00	0.00	1	
	save_data	5.08	0.00	0.00	1	
	init_data	4.23	0.00	0.00	1	
	init_bss	2.86	0.00	0.00	1	
Task1 508.88 mJ total 48.69 %	cache_on	8.82	0.00	0.01	1	
	win_unf_trap	6.09	1.16	9.43	1999	
	OSDisableInt	0.98	0.09	0.82	1000	
	OSEnableInt	1.07	0.10	0.92	1000	
	OSSemPend	6.00	0.57	4.56	999	
	104.59 mJ total 10.01 %	win_unf_trap	0.94	0.18	1.56	1999
		OSDisableInt	0.94	0.18	1.56	1999
		OSEnableInt	13.07	1.25	9.89	999
		OSEventTaskWait	66.44	6.35	51.95	999
	OSSemPost	0.96	0.09	0.78	1000	
	9.82 mJ total 0.94 %	OSDisableInt	0.98	0.09	0.81	1000
		OSEnableInt	0.98	0.09	0.81	1000
	4.62 mJ total 0.44 %	OSTimeGet	0.84	0.08	0.66	1000
		OSDisableInt	0.98	0.09	0.81	1000
	0.29 mJ total 0.03 %	CPUInit	3.52	0.00	0.00	1
exceptionHandler		15.51	0.02	0.17	15	
368.07 mJ total 35.22 %	printf	6.18	0.59	4.87	1000	
	vfprintf	355.04	33.97	257.55	1000	

## Example power-efficient change to RTOS

- Small changes can greatly improve RTOS power consumption
- $\mu\text{C}/\text{OS-II}$  tracks processor loading by incrementing a counter when idle
- However, this is not a good low-power design decision
- NOPs have lower power than add or increment instructions
- Sleep mode has *much* lower power
- Can disable loading counter and use NOPs or sleep mode

## Example power-efficient change to RTOS

- Alternatively, can use timer-based sampling
  - Normally NOP or sleep when idle
  - Wake up on timer ticks
  - Sample highest non-timer ISR task
  - If it's the idle task, increment a counter
  - Can dramatically reduce power consumption without losing functionality

## RTOS Conclusions

- Demonstrated that RTOS significantly impacts power
- RTOS power analysis can improve application software design
- Applications
  - Low-power RTOS design
  - Energy-efficient software architecture
  - Consider RTOS effects during system design

## Reference

Kaushik Ghosh, Bodhisattwa Mukherjee, and Karsten Schwan. A survey of real-time operating systems. Technical report, College of Computing, Georgia Institute of Technology, February 1994

## Scheduling and reliability reading

- Due 27 September: C. L. Liu and James W. Layland. Scheduling algorithms for multiprogramming in a hard-real-time environment. *J. of the ACM*, 20(1):46–61, January 1973.
- Due 29 September: Robert P. Dick. Reliability, thermal, and power modeling and optimization. In *Proc. Int. Conf. Computer-Aided Design*, pages 181–184, November 2010.
- Due 4 October: Yu-Kwong Kwok and Ishfaq Ahmad. Benchmarking and comparison of the task graph scheduling algorithms. *J. of Parallel and Distributed Computing*, 59(3):381–422, 1999.
- Due 6 October: L. Yang, Robert P. Dick, Haris Lekatsas, and Srimat Chakradhar. High-performance operating system controlled on-line memory compression. *ACM Trans. Embedded Computing Systems*, 9(4):30:1–30:28, March 2010.

## Upcoming topic

Embedded system memory hierarchies.